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Multidimensional Poverty Rankings based on Pareto Principle: A Practical Extension

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Pareto Principle: A Practical Extension

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Abstract

This paper proposes a ranking method of multidimensional poverty and extends it aiming to enhance its practical utility. While our original ranking method that assumes non-comparability among different dimensions of poverty succeeds in eliminating some implicit arbitrariness in existing ranking, it also confronts a disadvantage that a nonnegligible number of objectives (countries) are ranked at the same level. In order to improve this disadvantage, we propose an extended ranking method, where we allow the data to have a certain range of bandwidth. The introduction of bandwidth improves the usefulness of our ranking in the sense that it decreases the number of countries with the same rank. In addition, a simulation exercise shows that this extension also improves the robustness of the ranking against measurement errors.

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1 Introduction

This paper focuses on issues of multidimensional poverty measurement and ranking. A multidimensional poverty approach regards poverty not only as an economical connotation but also as a multifaceted one including various non-economical factors such as health, education, social exclusion and safety.

Literature on multidimensional poverty measurement can be traced back to early contributions like the physical quality of life index by Morris (1979), the deprivation index by Townsend (Townsend et. al. 1989), and the quality of life index by Dasgupta and Weale (1992). However, only in recent years have a number of studies tried to establish theory-based conceptions and methods to measure multidimensional poverty, based on the pioneering works.

Existing studies in this field can be broadly classified into two strands: statistical and non-statistical approaches. In the former, some sort of latent variable models are often employed. A latent variable model regards multidimensional poverty as an unobserved endogenous variable determined by several exogenous variables such as social, political and institutional factors. This kind of statistical analysis enables us to investigate the causal relationship among different dimensions of poverty.¹

On the other hand, non-statistical approaches can be divided into a further two subcategories: the fuzzy set approach and the multidimensional poverty ordering approach. The former explicitly takes into account the vagueness of multidimensional poverty. The

¹For more details on this topic, see Krishnakumar and Ballon (2008), Asselin (2009) and Kuklys (2005).

terms 'the poor' and 'the non-poor' may bring some ambiguity, even in the context of unidimensional (e.g. income-based) poverty. Despite this, a number of studies dichotomize the poor and non-poor by a sole poverty line. The fuzzy set approach aims to capture this ambiguity by employing so-called 'membership functions' that describe the degree of poverty, and succeeds in dealing with the dynamics of poverty (Qizilbash, 2006; Betti et al., 2008). The multidimensional poverty ordering approach is inspired by a pioneering work on the characterization of poverty index by Sen (1976). This approach consists of two stages. In the first, who is poor and to what extent are determined. For a set of individuals, the subset to which the poor belong is defined and the level of poverty for the set is expressed as an index value. Such poverty indices are usually characterized by an axiomatic basis, with aggregation of the shortfalls of the poor falling below a certain poverty line. The next stage provides some kinds of ranking rules to order sets of individuals in accordance with the level of multidimensional poverty. The majority adopt stochastic dominance criteria or its applications (Chakravarty and Bourguignon 2002; Tsui, 2002; Velez and Robles, 2008).

With these studies taken as the starting point, this paper proposes an alternative ranking methodology for multidimensional poverty. Whereas our method can be classified as a multidimensional poverty ordering approach, the approach in this paper can be distinguished from others. Our approach is based on the significant assumption that we allow the non-comparability of one dimension of multidimensional poverty with another. This reflects the implicit belief that we can never compare the value of poverties over dimensions because a distinct dimension represents a distinct aspect of poverty. However, this belief also highlights a practical disadvantage of the ranking, whereby many objectives are ranked at the same level. In typical rankings, one objective corresponds to one rank, but multiple objectives may have equivalent rank in our approach. Consequently, the ranking yielded by our approach is possibly coarser than other typical rankings in the sense that many non-comparable objectives remain. Due to this disadvantage, dominance order ranking is subject to the criticism that it lacks practical utility, despite successfully eliminating implicit arbitrariness in existing measures.

In order to alleviate the coarseness of the ranking, we propose an extended ranking method, where we allow the data to have a certain range of bandwidth. The introduction of bandwidth is also interpretable as neglecting a certain range of differences between the data, and doing this turns many countries from non-comparable to comparable. Thus, the extended ranking method can improve the usefulness of the ranking in the sense that it decreases the number of countries with the same rank. In addition, this extension has a secondary effect: the extended method of ranking is more robust to measurement errors than the original method, since allowing the data to have a bandwidth is equivalent to presuming that the data have measurement errors. We will confirm this by conducting a simulation exercise.

The rest of this paper is organized as follows. The next section reviews the framework of the dominance order ranking and its extension. Section 3 examines the ranking results derived from the original and extended method, and shows the result of a simulation exercise. We conclude in the final section.

2 Dominance Order Ranking and Its Practical Extension

2.1 Reviewing the dominance order ranking

Before proceeding to explain the extended method of the dominance order ranking proposed by Michinaka (2009), we review the concept of Michinaka's ranking method and its advantages and drawbacks.² Let us assume that the level of multidimensional poverty for each country is expressed by the multidimensional development profile, which is a bundle of the values of multiple indicators representing the level of poverty, such as GDP per capita, infant mortality rate, and adult literacy rate. These indicators are common among all objectives (e.g. individuals, countries or societies) to be ranked. We also assume that the value of each indicator is a real positive number. Note that the basis for the information in our approach is the degree of development, although most existing approaches use the degree of deprivation for the same basis, based on some sort of poverty lines. This is why we refer to a 'multidimensional development profile' instead of 'multidimensional poverty profile.' As stated in the previous section, we eliminate the implicit arbitrariness included in all poverty lines.

²Michinaka (2009) proposes three different ranking methods based on the concept of the Pareto dominance: minimal order ranking (MINOR), maximal order ranking (MAXOR) and Pareto dominance order ranking (PDOR). In what follows, unless otherwise noted, we use the term 'dominance order ranking' to refer to 'MAXOR.'

The dominance order ranking is formulated as follows. Let C be the set of countries and I be the set of the poverty indicators. The number of elements in C and I is denoted by $\sharp C$ and $\sharp I$, respectably. The level of multidimensional development for any countries in C is expressed as $f(c) = (f_c^i)_{i \in I}$ where $f(\cdot)$ is a mapping that assigns the $\sharp I$ -dimensional poverty level to a country c in C.

Regarding binary relations determining a ranking, we let \succeq denote the binary relation on C that means 'at least as developed as,' defined as $c \succeq \hat{c} :\Leftrightarrow \forall c, \hat{c} \in C \& \forall i \in I, f_c^i \ge f_c^i$. Corresponding to this binary relation, we now define the three binary relations on C; (1) \succ means 'strictly more developed than' and is defined as $\forall c, \hat{c} \in C, \& \forall i \in I, c \succ$ $\hat{c} :\Leftrightarrow f_c^i \ge f_c^i \& \exists f_c^i$ such that $f_c^i > f_c^i$, (2) \sim means 'as developed as' and is defined as $c \sim \hat{c} :\Leftrightarrow \forall c, \hat{c} \in C, \& \forall i \in I, f_c^i = f_c^i$, and (3) \bowtie means 'non-comparable' and is defined as $c \bowtie \hat{c} :\Leftrightarrow \forall c, \hat{c} \in C, \exists i \in I$ such that $f_c^i > f_c^i \& \exists j \in I$ such that $f_c^j < f_c^j$. \succ and \sim are the asymmetric and symmetric factors of \succeq , and \bowtie is an incomparability relationship corresponding to \succeq : namely $c \bowtie \hat{c} \Leftrightarrow \neg (c \succeq \hat{c}) \& \neg (\hat{c} \succeq c)$. ³ Since the binary relation \succ describes Pareto dominance, if $c \succ \hat{c} (\forall c, \hat{c} \in C)$, then c is interpreted as dominating \hat{c} .

Using the above binary relations, we now define the dominance order ranking. First of all, we define a maximal set of X as follows:

$$\overline{M}(X,\succ) = \{x \mid x \in X \& \text{ there is no } y \in X \text{ such that } y \succ x\}$$

Utilizing the concept of maximal sets, the dominance order ranking is generated by repeating the following steps:

³The symbol \neg denotes the negation of a logical statement.

(step 1) Make the maximal set on C, and call it \overline{M}_1 , and define the (relative) complement of \overline{M}_1 in C ($C \setminus \overline{M}_1$) as C_1 .

(step 2) Again, make the maximal set \overline{M}_2 on C_1 , namely,

 $\overline{M}_2(C_1, \succ) = \{c \mid c \in C_1 \& \text{ there is no } \hat{c} \in C_1 \text{ such that } \hat{c} \succ c\}.$ and define $C_1 \setminus \overline{M}_2$) as C_2 .

(step 3) In the same manner, make the maximal set \overline{M}_r on C_{r-1} until $C_{r-1} \setminus \overline{M}_r = \emptyset$. Consequently, this procedure yields a sequence of maximal sets, namely, $\overline{M}_1, \overline{M}_2, \ldots$, $\overline{M}_r, \ldots, \overline{M}_R$. The subscript r of \overline{M}_r corresponds to the rank of the countries belonging to the maximal set.

Thus, the processes of making a dominance order ranking are equivalent to that of making a partition of a set. These processes require no aggregation or indexation of different development indices. In this sense, the dominance order ranking succeeds in eliminating the implicit arbitrariness associated with the aggregation, and this is attributed to the fact that the ranking is based solely on the ordinal relationship between the values of indices.

However, owing to this fundamental non-comparability between different indices, the dominance order ranking has the drawback of 'tie-full tendency.' It means many countries are ranked at the same rank, and things will worsen as the dimension of development or poverty indices ($\sharp I$) increases.⁴

Due to this disadvantage, the dominance order ranking is subject to the criticism that it lacks practical utility even though it is convincing, less arbitrary and intuitively

⁴Regarding other advantages and disadvantages, see Michinaka (2009).

understandable. In the next subsection, we propose a method to improve the drawback of the tie-full tendency.

2.2 Allowing a Bandwidth of Data

For simplicity's sake, consider a case where there are only two indices $(\sharp I = 2)$ denoted by x and y. Figure 1 depicts the way of the dominance order ranking. Focusing on country D in the first panel, the tie-full tendency is related to the shaded square areas lying to the northwest and southeast of D. We refer to these areas as 'non-comparable areas' of D, since countries B, C, E and G in these areas are non-comparable to D. The tie-full tendency is mainly attributed to these non-comparable areas, and consequently, reducing the area is largely equivalent to improving the tie-full tendency,

In fact, there are several ways to reduce the area. For instance, approaches admitting a cardinality among values of multiple indicators, like the Human Development Index (HDI), mean arbitrary weights are placed on each indicator. Consequently, any pairs of $f(c) = (f_c^i)_{i \in I}$ and $f(c) = (f_c^i)_{i \in I}$ for all $c, \hat{c} \in C$ are comparable since $f(c) = (f_c^i)_{i \in I}$ for all $c \in C$ can be a scalar as an aggregated index value (in short, there is no non-comparable area).

One of the ways to decrease in a dimension of the non-comparable areas, while maintaining the advantage of the dominance order ranking, is to allow the data of the indicators to have a certain range of bandwidth (the second panel of Figure 1). This is also interpretable as neglecting a certain range of differences between the values of indicators, or equivalent to presuming that the data have measurement errors. Considering the fact that country-level data potentially contain a certain level of measurement errors, allowing data to have a bandwidth (as d^x and d^y in the second panel) can be justified to some extent and is also plausible from a practical perspective. As the figure shows, doing this makes the area decreased, and means countries C and E can escape from the non-comparable areas of D.

At the same time, however, this approach also has a weakness: the existence of the bandwidth generates an area within which all values are regarded as indifferent. In the second panel of Figure 1. this is depicted as the area bounded by the solid line and referred to as 'indifference area' of D. Due to this area, the country F is reclassified from the category of comparable to indifferent.

Thus, the introduction of a bandwidth has an advantage and disadvantage: whereas the number of countries reclassified from the category of non-comparable (i.e. $c \bowtie \hat{c}$) to comparable (i.e. $c \succ \hat{c}$ or $\hat{c} \succ c$), denoted by #M, increases, the same applies to that moving from comparable to indifferent (i.e. $c \sim \hat{c}$), as denoted by #D. Regarding #M and #D as the benefit and cost of introducing a bandwidth, an optimal bandwidth for index *i* can be obtained as the solution to the following maximization problem:

$$\widehat{d}^{i} = \arg \max\{\sum_{c \in C} \# M_{c}(d^{i}) - \# D_{c}(d^{i})\}\$$

In this paper, we allow the bandwidth to vary among countries by setting $d_c^i = f_c^i \times r_i$ (but r_i is common for all countries), and choose an optimal r_i in the same manner.

Subsequently, for all $c, c \in C$ and $i \in I, f_c^i$ and f_c^i are regarded as equivalent if $|f_c^i - f_c^i| \leq d_c^i$. In other words, if $|f_c^i - f_c^i| \leq d_c^i$, then the development level of c and that of \hat{c} are regarded as indifferent. In the next section, we present the ranking result obtained through this procedure and compared with the result of the standard dominance order ranking.

3 Ranking Results and a Simulation Exercise

3.1 Results of the ranking methods

In this section, we show the ranking results obtained through the dominance order ranking and the extended ranking. We adopt the data used to calculate the HDI, which is one of the most consulted multidimensional poverty measures. The HDI is a composite index consisting of four indicators; life expectancy at birth, the adult literacy rate, the combined gross enrolment ratio for primary, secondary and tertiary schools,,and GDP per capita. The data of these indicators for 182 countries were used to calculate the HDI in 2009.

Using this HDI 2009 data, we show two ranking results generated by the ranking methodologies proposed in the previous section, namely, the dominance order ranking and the extended dominance order ranking (See Table 1). Concerning the extended ranking, the calculated result of the optimal value of r is 0.1073. While the HDI ranking in 2009 for 182 countries is a complete ranking from the first (Norway) to the 182nd (Niger), a number of countries are ranked identically in terms of both the dominance order ranking and the extended dominance order ranking. Consequently, the former manages to rank the 182

countries into only seventeen groups from first to last place. In this ranking, twenty-two countries are ranked into the top bracket (the rank of 69, namely the seventh place group) and at the least, a country (the rank of 182nd, namely the bottom place group). While the latter still sees several countries ranked the same, it succeeds in decreasing the numbers. The extended ranking ranks 182 countries to forty groups. Only nine countries are ranked at the top (the rank of 9th, namely the second place group) and at the opposite end, a country (the rank of 181st and 182nd, namely the bottom and next group). In other words, the extended ranking succeeds to improve the practical utility in the sense that it alleviates the coarseness of the original dominance order ranking.

As stated in the previous section, this extension brings both benefit and cost to the original ranking. The benefit is the fact that neglecting of slight difference among data values possibly changes some binary relations non-comparable to comparable. Conversely, the cost of this neglect also possibly changes some binary relations from comparable to indifferent. For an example of the former case, see the Czech Republic and Albania ranked 43rd in the dominance order ranking. The level of multidimensional poverty of the former is $(f_{CR}^i)_{i\in I} = (76.4., 99.0, 83.4, 24144)$ while that of the latter is $(f_{ALB}^i)_{i\in I} = (76.5, 99.0, 67.8, 7041)$. These countries are ranked the same due to only a slight (0.1) difference in the value of life expectancy. The introduction of bandwidth will mean this slight difference can be neglected, while the ranks of these countries in extended ranking are quite different from each other (34th and 93rd). Likewise, for an instance of the latter, see Portugal ranked 34th in the dominance order ranking with $(f_{POR}^i)_{i \in I} = (78.6., 94.9, 88.8, 22765)$ dominates Chez Republic so that the former is ranked prior to the latter. Meanwhile, the introduction of bandwidth changes the binary relation on these countries from comparable to indifferent. Consequently, the ranks of these countries are the same (34th) in the extended ranking.

Our results shows that when we allow approximately a 10% difference in data value, the practical utility of the dominance order ranking is maximized, namely, the number of countries that have the same rank is minimized. It seems natural that we assume the existence of measurement error in any dataset. In particular, it is difficult to collect precise datasets in developing countries. With this in mind, acceptance of an error range of plus or minus 10% does not seem a quite unreasonable assumption.

3.2 A Simulation Exercise

As mentioned earlier, our extension has a secondary effect, whereby the extended method of ranking is more robust to measurement errors than the original method. To see this, a simulation exercise is implemented.

First of all, we assume that $\ln f_c^i = \mu_c^i + \epsilon_c^i$, rather than the true value μ_c^i , is observed, where ϵ_c^i is a random error. The random error may come from the measurement or other resources, and has i.i.d. $N(0, \sigma_i^2)$. Hence, we regard f_c^i as a log-normal random variable with mean $\exp(\mu_c^i + \frac{\sigma_i^2}{2})$ and variance $\exp(2\mu_c^i + \sigma_i^2) \{\exp(\sigma_i^2) - 1\}$.

We now consider the following measure ρ that indicates the extent to which the true value μ_c^i explains the observed value $\ln f_c^i$: $\rho = \frac{E[\mu_c^i - \bar{\mu}^i]^2}{E[\ln f_c^i - \bar{\mu}^i]^2}$. This measure, which is similar to the coefficient of determination (regression R^2) when regressing $\ln f_c^i$ on μ_c^i , ranges between zero and one, and as it assumes a larger value, the error ϵ_c^i has less influence on the observed value $\ln f_c^i$. Subsequently, an unbiased and consistent estimator of σ_i^2 for each ρ is calculated by:

$$\widehat{\sigma}_{i}^{2} = \frac{\sum (\ln f_{c}^{i} - \mu_{c}^{i})^{2}}{N} = \frac{\sum [(\ln f_{c}^{i} - \bar{\mu}^{i}) - (\mu_{c}^{i} - \bar{\mu}^{i})]^{2}}{N} = \frac{(1 - \rho) \sum (\ln f_{c}^{i} - \bar{\mu}^{i})^{2}}{N}, \forall i \in I \text{ and } \forall \rho \in I$$

Using this $\hat{\sigma}_i^2$, we simulate 100 runs of a (hypothetical) true value of f_c^i , denoted by z_c^i :

$$z_{c,t}^{i} = \exp\left(\mu_{c,t}^{i} + \frac{\hat{\sigma}_{i,\rho}^{2}}{2}\right) = \exp\{(\ln f_{c}^{i} - \epsilon_{c,t}^{i} + \frac{\hat{\sigma}_{i,\rho}^{2}}{2})\} = f_{c}^{i} \times \exp(-\epsilon_{c,t}^{i} + \frac{\hat{\sigma}_{i,\rho}^{2}}{2}),$$

where the additional subscript t means the t-th trial, and $\epsilon_{c,t}^i$ is drawn at random from $N(0, \hat{\sigma}_{i,\rho}^2)$. In each trial, using the hypothetical data z_c^i , we obtain ranking results based on the standard procedure and our 'with-bandwidth' procedure, and investigate the extent to which ranking results are sensitive to hypothetical (measurement) errors.

Figure 2 shows the results of the simulation exercise. As a measure to indicate the robustness of the ranking results, we employ the Spearman's and the Kendall's rank correlation coefficients between the ranking result, using the actual data and hypothetical data respectively. As the coefficients are close to unity, the results are interpreted as being robust to measurement errors. The figure shows that the coefficients of the extended method are significantly bigger than those of the original method. which indicates that our 'with-bandwidth' method is more robust to measurement errors than the original ranking method.

4 Conclusion

This paper proposed a ranking named the dominance order ranking, which is a method for ranking the levels of multidimensional poverty and extended it in order to improve its practical utility. This extended ranking is much finer than the original ranking. In addition, the extended ranking is more robust to measurement errors than the original.

While the dominance order ranking succeeds in eliminating some implicit arbitrariness in existing multidimensional poverty rankings, it has the disadvantage of a number of objectives being ranked the same. In other words, a number of objectives remain noncomparable. Due to this disadvantage, the dominance order ranking is criticized as lacking practical utility.

To enhance the practical utility, we introduce a new aspect that allows a certain range of measurement error in the data we use. Neglecting a slight disparity in the data value possibly decreases the number of countries with the same rank. We select the range of measurement errors that maximizes practical utility in the sense of minimizing the number of countries with the same rank. When we allow a difference of approximately 10.73% among data values, the practical utility is maximized and the number of ranks in ranking increased to forty from seventeen. This extension also enhanced the robustness to error in data and is shown by a simulation exercise.

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GDP per capita life expectancy adult literacy combined gross HDI (PPP\$) at birth enrolment ratio rate DOR EDOR country rank value rank value rank value rank rank value value 0.960 Luxembourg 79.4 99.0 79485 16 94.4 11 24 1 2 1 1 1 19 26 79.2 1 41 1 85382 1 0.951 Liechtenstein 99.0 86.8 3 0.971 Norway 12 80.5 1 99.0 8 98.6 5 53433 1 1 9 1 2 0.970 Australia 5 81.4 1 99.0 1 100.0 22 34923 19 35742 1 9 3 0.969 Iceland 3 81.7 1 99.0 13 96.0 1 9 4 0.966 Canada 11 80.6 1 99.0 99.3 18 35812 7 1 9 7 0.963 Sweden 8 80.8 1 99.0 17 94.3 16 36712 1 9 16 0.955 Denmark 34 78.2 1 99.0 1 100.0 17 36130 1 1 18 9 0.960 Switzerland 3 81.7 99.0 49 82.7 13 40658 1 23 10 0.960 Japan 1 82.7 1 99.0 42 86.6 26 33632 0.944 Hong Kong, China 2 1 23 24 82.2 76 88 74.4 11 42306 94.6 (SAR) 12 3 33 0.910 Qatar 48 75.5 86 93.1 57 80.4 3 74882 12 5 5 0.965 Ireland 19 79.7 99.0 10 97.6 10 44613 1 28 79.1 12 5 1 99.0 21 9 45592 13 0.956 United States 92.4 7 49704 12 5 23 0.944 Singapore 14 80.2 79 94.4 46 85.0 12 5 38 94.9 30 0.920 Brunei Darussalam 77.0 73 74 77.7 6 50200 12 9 17 79.8 1 99.0 11 97.5 14 38694 6 0.964 Netherlands 1 9 12 14 0.955 Austria 16 79.9 99.0 27 90.5 15 37370 12 9 35 0.903 United Arab Emirates 37 77.3 107 99 90.0 71.4 4 54626 12 81.0 25 33674 18 8 0.961 France 7 1 99.0 15 95.4 22 12 1 18 12 0.959 Finland 79.5 99.0 1 100.0 23 34526 12 15 0.955 Spain 9 80.7 53 97.9 12 96.5 27 31560 18 12 31 0.916 Kuwait 36 77.5 78 94.5 100 72.6 8 47812 18 12 23 98.9 29 30353 0.951 Italy 81.1 47 23 91.8 18 6 12 23 20 0.950 New Zealand 15 80.1 1 99.0 1 100.0 32 27336 12 30 28 0.934 Andorra 12 80.5 1 99.0 127 65.1 12 41235 27 22 1 21 34935 9 17 0.953 Belgium 79.5 99.0 17 94.3 0.947 United Kingdom 27 23 21 25 79.3 1 99.0 34 89.2 20 35130 37 27 23 22 0.947 Germany 18 79.8 1 99.0 88.1 24 34401 27 23 25 0.942 Greece 29 79.1 97.1 1 31 28517 60 100.0 79.2 9 27 30 26 0.937 Korea (Republic of) 26 99.0 98.5 35 24801 1 34 26315 27 30 27 0.935 Israel 9 80.7 60 97.1 33 89.9 27 51 51 0.863 Cuba 33 78.5 99.0 100.0 95 6876 1 1 33 26753 29 34 78.2 1 20 34 30 0.929 Slovenia 99.0 92.8 34 34 34 0.909 Portugal 31 78.6 73 94.9 35 88.8 42 22765 34 34 38 0.902 Malta 20 79.6 89 92.4 54 81.3 39 23080 75.6 30 29723 34 47 28 39 0.895 Bahrain 88.8 90.4 34 105 0.914 Cyprus 20 34 39 32 79.6 56 97.7 75 77.6 36 24789 34 37 38 77.0 99.0 19 92.9 48 17956 39 0.903 Barbados 1 34 39 118 0.719 Equatorial Guinea 168 49.9 113 87.0 133 62.0 28 30627 34 55 0.847 Libyan Arab 64 73.8 114 44 86.8 14 95.8 57 14364 34 44 0.878 Chile 32 78.5 96.5 50 82.5 59 13880 58 66 43 34 36 0.903 Czech Republic 42 76.4 1 99.0 48 83.4 37 24144 43 1 43 20361 34 40 0.883 Estonia 74 72.9 99.0 25 91.2 43 39 69 73.3 47 43 0.879 Hungary 98.9 30 90.2 46 18755 43 39 46 0.870 Lithuania 91 71.8 1 99.0 22 92.3 49 17575 43 53 43 44 50 0.865 Uruguay 76.1 97.9 26 90.9 70 11216 48 43 51 41 0.880 Poland 75.5 1 99.0 39 87.7 53 15987 43 58 49 0.866 Argentina 53 75.2 57 97.6 36 88.6 62 13238 43 72 54 0.854 Costa Rica 30 78.7 70 95.9 98 73.0 73 10842 73 43 0.814 Dominica 40 76.9 88.0 65 78.5 83 81 108 7893 99.0 43 93 70 0.818 Albania 41 76.5 122 67.8 1 93 7041 53 44 42 0.880 Slovakia 56 74.6 1 99.0 56 80.5 45 20076

Table 1: Dominance Order Ranking, Extend Dominance Order Ranking and Human Development Index

Table 1(continued)

DOR	EDOR	HDI		country	life expectancy at birth		adult literacy rate		combined gross enrolment ratio		GDP per capita (PPP\$)	
		rank	value		rank	value	rank	value	rank	value	rank	value
53	44	47	0.868	Antigua and Barbuda	84	72.2	1	99.0	45	85.6	47	18691
53	44	59	0.843	Saudi Arabia	77	72.7	117	85.0	65	78.5	40	22935
53	44	64	0.837	Trinidad and Tobago	110	69.2	49	98.7	137	61.1	38	23507
53	44	68	0.826	Belarus	111	69.0	1	99.0	28	90.4	74	10841
53	51	48	0.866	Latvia	83	72.3	1	99.0	30	90.2	51	16377
53	51	52	0.856	Bahamas	71	73.2	71	95.8	103	71.8	44	20253
53	51	56	0.846	Oman	48	/5.5	118	84.4	118	68.2	41	22816
53	51	57	0.845	Seychelles	/6	72.8	92	91.8	52	82.2	50	16394
53 52	50 50	02	0.004	Croatia	130	04.9 76.0	10	99.0	<u></u> 77	91.4	1Z 52	10003
53	00 61	40	0.071	Mexico	44	76.0	49	90.7	// 58	80.2	58	1/10/
- 55	01	55	0.034	Venezuela (Bolivarian	44	70.0	07	92.0	50	00.2		14104
53	64	58	0.844	Republic of)	66	73.6	72	95.2	44	85.9	65	12156
53	64	60	0.840	Panama	48	75.5	83	93.4	59	79.7	67	11391
53	64	61	0.840	Bulgaria	72	73.1	52	98.3	51	82.4	69	11222
53	72	78	0.806	Peru	73	73.0	102	89.6	37	88.1	85	7836
69	61	62	0.838	Saint Kitts and Nevis	84	72.2	55	97.8	96	73.1	56	14481
69	61	71	0.817	Russian Federation	122	66.2	1	99.0	53	81.9	55	14690
69	64	63	0.837	Romania	80	72.5	5/	97.6	61	/9.2	64	12369
69	64	103	0.755	Gabon	144	60.1 74.4	115	86.Z	55	80.7	54	15167
69	69	00	0.829	Ivialaysia Brozil	00 01	74.1	91	91.9	105	71.5	70	13318
60	09 72	75	0.013	Montonogra	04 61	74.0	99	90.0	40	01.Z	19	9007
60	77	60 60	0.004	Spint Lucia	10	74.0	<u>07</u> 75	90.4	00 77	74.3	00 77	0786
60	77	85	0.021	Likraino	116	68.2	1	94.0 00 N	32	90.0	Q/	6014
69	81	77	0.730	Colombia	77	72.7	88	92.7	63	79.0	81	8587
69	84	72	0.817	Macedonia (the	58	74.1	62	97.0	113	70.1	80	9096
60	8/	80	0.806	Foundor	55	75.0	0/	01.0	73	77.8	01	7//0
69	87	74	0.813	Grenada	52	75.3		96.0	96	73.1	92	7344
69	87	76	0.812	Bosnia and	54	75.1	65	96.7	114	69.0	87	7764
60	87	86	0 787		107	70.0	1	00.0	12/	66.2	8/	7851
60	07	00	0.707	Rolizo	46	76.0	134	<u> </u>	67	78.3	04 06	6734
69	96	84	0.798	Armenia	0 66	73.6	104	99.0	85	70.5	100	5693
69	101	89	0.730	Georgia	96	71.6	1	99.0	81	74.0	110	4662
69	101	98	0.769	Tunisia	64	73.8	130	77.7	83	76.2	90	7520
69	107	99	0.768	Tonga	92	71.7	1	99.0	70	78.0	120	3748
69	107	105	0.751	Philippines	96	71.6	83	93.4	60	79.6	124	3406
69	124	110	0.737	Occupied Palestinian Territories	69	73.3	82	93.8	67	78.3	135	2243
91	69	79	0.806	Turkey	92	71.7	106	88.7	109	71.1	63	12955
91	72	81	0.804	Mauritius	88	72.1	112	87.4	79	76.9	68	11296
91	72	125	0.694	Botswana	160	53.4	122	82.9	111	70.6	60	13604
91	77	67	0.826	Serbia	63	73.9	67	96.4	86	74.5	75	10248
91	77	83	0.803	Lebanon	90	71.9	102	89.6	70	78.0	76	10109
91	84	87	0.783	Thailand	113	68.7	81	94.1	70	78.0	82	8135
91	87	100	0.766	Jamaica	92	71.7	116	86.0	69	78.1	98	6079
91	93	96	0.770	Jordan	81	72.4	93	91.1	64	78.7	107	4901
91	96	95	0.771	Maldives	102	71.1	62	97.0	108	71.3	104	5196
91	96	113	0.729	Bolivia	128	65.4	96	90.7	43	86.0	117	4206
91	101	94	0.771	Samoa	98	71.4	49	98.7	90	74.1	113	4467
91	101	109	0.739	Turkmenistan	132	64.6	1	99.0	92	73.9	106	4953
91	107	102	0.759	Sri Lanka	61	74.0	95	90.8	116	68.7	116	4243

Table 1 (continued)

DOR	EDOR	HDI		country	life expectancy at birth		adult literacy rate		combined gross enrolment ratio		GDP per capita (PPP\$)	
		rank	value	country	rank	value	rank	value	rank	value	rank	value
91	114	107	0.742	Syrian Arab Republic	58	74.1	121	83.1	125	65.7	112	4511
91	114	115	0.727	Mongolia	122	66.2	59	97.3	61	79.2	125	3236
91	119	114	0.729	Guyana	119	66.5	1	99.0	47	83.9	127	2782
91	119	11/	0.720	Moldova	115	68.3	1	99.0	104	/1.6	131	2551
91	124	116	0.725		5/	74.3	98	90.3	130	62.3	129	2600
110	81	88	0.710	Iran (Islamic Republic	101	67.6 71.2	123	99.0 82.3	<u>76</u> 95	73.2	71	10955
110	87	97	0 769	Suriname	112	68.8	97	90.4	89	74.3	86	7813
110	87	129	0.683	South Africa	164	51.5	108	88.0	80	76.8	78	9757
110	96	91	0.772	Saint Vincent and the Grenadines	98	71.4	107	88.1	115	68.9	89	7691
110	96	92	0.772	China	74	72.9	85	93.3	116	68.7	102	5383
110	101	90	0.777	Dominican Republic	81	72.4	104	89.1	94	73.5	97	6706
110	101	104	0.754	Algeria	84	72.2	133	75.4	93	73.6	88	7740
110	107	101	0.761	Paraguay	92	71.7	76	94.6	101	72.1	114	4433
110	107	106	0.747	El Salvador	100	/1.3	125	82.0	91	74.0	99	5804
110	107	123	0.703	Egypt	108	69.9	149	66.4	82	76.4	103	5349
110	114	112	0.732	Honduras	89	67.6	120	83.0	<u>84</u>	74.8	119	3/90
110	12/	124	0.710	Nicaraqua	77	07.0	120	90.9 78.0	99	72.1	130	2420
110	124	124	0.099	Tajikistan	120	66.4	123	00.0	110	70.0	1/5	1753
124	107	108	0.000	Fiii	113	68.7	79	94.4	105	70.3	145	4304
124	114	111	0.734	Indonesia	105	70.5	90	92.0	118	68.2	121	3712
124	114	128	0.686	Namibia	143	60.4	108	88.0	123	67.2	105	5155
124	119	122	0.704	Guatemala	106	70.1	138	73.2	112	70.5	111	4562
124	119	143	0.564	Angola	178	46.5	147	67.4	126	65.3	101	5385
124	124	130	0.654	Morocco	104	71.0	162	55.6	138	61.0	118	4108
124	124	132	0.619	Bhutan	126	65.7	167	52.8	152	54.1	108	4837
124	131	121	0.708	Cape Verde	102	71.1	119	83.8	120	68.1	126	3041
132	124	126	0.693	Vanuatu	108	69.9	128	78.1	130	62.3	122	3666
132	124	142	0.572	Swaziland	179	45.3	127	79.6	141	60.1	109	4789
132	131	136	0.601		159	53.5	126	81.1	144	58.6	123	3511
132	130	131	0.651	Sao Tome and	129	61.2	101	87.9	120	<u>68.1</u>	149	1638
132	134	130	0.000	India	13/	63.4	101	69.9 66.0	149	20.3 61.0	100	904
137	134	133	0.612	Lao People's	134	64.6	139	72.7	142	59.6	136	2165
137	139	137	0.593	Cambodia	142	60.6	132	76.3	145	58.5	144	1802
137	139	141	0.572	Pakistan	122	66.2	164	54.2	174	39.3	132	2496
137	139	156	0.514	Lesotho	180	44.9	124	82.2	135	61.5	151	1541
137	144	135	0.610	Solomon Islands	125	65.8	131	76.6	162	49.7	146	1725
137	144	144	0.553	Nepal	121	66.3	160	56.5	140	60.8	166	1049
137	144	145	0.543	Madagascar	145	59.9	143	70.7	136	61.3	167	932
137	144	147	0.541	Kenya	158	53.6	136	73.6	142	59.6	150	1542
137	152	162	0.489	Timor-Leste	140	60.7	168	50.1	129	63.2	174	717
137	152	164	0.481	Zambia	181	44.5	144	70.6	128	63.3	153	1358
137	159	146	0.543	Bangladesh	126	65.7	165	53.5	158	52.1	156	1241
137	159	157	0.514	Uganda	163	51.9	136	73.6	130	62.3	164	1059
137	163	160	0.493	Malawi	162	52.4	142	71.8	134	61.9	173	761
151	136	140	0.575	Yemen	135	62.5	158	58.9	151	54.4	134	2335
151	139	153	0.523	Cameroon	165	50.9	146	67.9	156	52.3	137	2128

Table 1 (continued)

DOR	EDOR	HDI		country		life expectancy at birth		adult literacy rate		combined gross enrolment ratio		GDP per capita (PPP\$)	
		rank	value		rank	value	rank	value	rank	value	rank	value	
151	144	155	0.520	Djibouti	155	55.1	145	70.3	182	25.5	140	2061	
151	144	158	0.511	Nigeria	173	47.7	141	72.0	154	53.0	142	1969	
151	152	139	0.576	Comoros	130	64.9	134	75.1	169	46.4	160	1143	
151	152	149	0.532	Haiti	138	61.0	155	62.1	158	52.1	159	1155	
151	152	150	0.531	Sudan	147	57.9	156	60.9	173	39.9	138	2086	
151	152	151	0.530	Tanzania (United Republic of)	156	55.0	140	72.3	147	57.3	158	1208	
151	152	152	0.526	Ghana	152	56.5	151	65.0	148	56.5	154	1334	
151	168	169	0.442	Liberia	147	57.9	163	55.5	146	57.6	180	362	
161	144	148	0.541	Papua New Guinea	140	60.7	159	57.8	172	40.7	139	2084	
161	144	154	0.520	Mauritania	151	56.6	161	55.8	160	50.6	143	1927	
161	159	165	0.472	Eritrea	146	59.2	154	64.2	178	33.3	178	626	
161	163	159	0.499	Togo	136	62.2	166	53.2	153	53.9	171	788	
161	163	161	0.492	Benin	138	61.0	174	40.5	155	52.4	155	1312	
161	163	167	0.460	Rwanda	169	49.7	152	64.9	157	52.2	169	866	
161	168	172	0.402	Mozambique	172	47.8	171	44.4	150	54.8	170	802	
161	168	176	0.389	Congo (Democratic Republic of the)	174	47.6	148	67.2	166	48.2	182	298	
161	174	174	0.394	Burundi	167	50.1	157	59.3	164	49.0	181	341	
170	159	163	0.484	Cote d'Ivoire	150	56.8	169	48.7	175	37.5	147	1690	
170	163	166	0.464	Senegal	154	55.4	173	41.9	171	41.2	148	1666	
170	168	168	0.456	Gambia	153	55.7	172	42.5	168	46.8	157	1225	
170	168	173	0.396	Guinea-Bissau	175	47.5	153	64.6	176	36.6	179	477	
170	174	170	0.435	Guinea	149	57.3	178	29.5	163	49.3	161	1140	
170	174	171	0.414	Ethiopia	157	54.7	176	35.9	164	49.0	172	779	
170	178	181	0.352	Afghanistan	182	43.6	181	28.0	161	50.1	165	1054	
177	168	175	0.392	Chad	170	48.6	177	31.8	177	36.5	152	1477	
177	174	179	0.369	Central African Republic	177	46.7	170	48.6	180	28.6	175	713	
177	178	178	0.371	Mali	171	48.1	182	26.2	167	46.9	163	1083	
177	178	180	0.365	Sierra Leone	176	47.3	175	38.1	170	44.6	176	679	
177	181	177	0.389	Burkina Faso	161	52.7	179	28.7	179	32.8	162	1124	
182	182	182	0.340	Niger	166	50.8	179	28.7	181	27.2	177	627	

Notes:

1. DOR: the dominance order ranking EDOR: the extended dominance order ranking

HDI: the Human Development Index

2. This table was made by the author based on the data on the Human Development Report 2009 (UNDP 2009).

3. The HDI rank is determined using HDI values to the sixth decimal point.

4. The most of developed countries do not maintain the statistics of adult literacy rate, and the UNDP applies 99.0% to these countries. To keep a consistency with these countries, the author applied 99.0% to the countries that achieved over 99.0% adult literacy rate.

5. Though the value of combined gross enrolment ratio of some countries are over 100.0 in the HDR 2009, the author applied 100.0 to these countries.

Figure 1: Illustrative drawing of the dominance order ranking method



A: Comparable and non-comparable areas

Note: *y* and *x* on the vertical and horizontal axes are indicators representing the level of poverty, and capital letters A to H indicate countries. The shaded areas in both panels are 'non-comparable areas' of country D, and the area bounded by the solid line in the second panel is referred to as 'indifference area' of D.



Figure 2: Results of a simulation exercise

Note: Correlation coefficients are on the vertical axis, and ρ , which indicates the influence of the hypothetical error, is on the horizontal axis. Simulations are implemented at 0.01 unit intervals for $\rho \in [0.9, 0.99]$.